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NEPS TECHNICAL REPORT FOR PHYSICS COMPETENCE: SCALING RESULTS FOR THE ADDITIONAL STUDY THURINGIA

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NEPS Technical Report for Physics Competence: Scaling Results for the Additional Study Thuringia

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NEPS Technical Report for Physics Competence: Scaling Results for the Additional Study Thuringia

Abstract

The National Educational Panel Study (NEPS) is aimed at investigating the development of competences across the entire life span. It also develops tests for assessing different competence domains. In order to evaluate the quality of these competence tests, a wide range of item response theory (IRT) analyses were carried out. This paper describes the data and results of analyses of the physics competence test that was used in the additional study Thuringia. In sum, 2,254 students took the test in two waves. The physics competence test consisted of 64 items (distributed among nine booklets). A Rasch model was used to scale the data. Item fit statistics and differential item functioning were investigated. The results showed that a subset of the items exhibited good item fit and measurement invariance across various groups. The paper also provides some information about the data available in the Scientific Use File as well as Con-Quest- and TAM-syntaxes for scaling the data.

Keywords

item response theory, scaling, physics competence, scientific use file

Content

Abstract 2

1 Introduction 4

2 Testing Physics Competence 4

3 Data 8

4 Analyses..... 8

 4.1 Missing Responses..... 8

 4.2 Scaling Model 8

 4.3 Checking the Quality of the Scale..... 9

5 Results 10

 5.1 Missing Responses..... 10

 5.1.1 Missing responses per person..... 10

 5.1.2 Missing responses per item 12

 5.2 Parameter Estimates 12

 5.2.1 Item parameters 12

 5.2.2 Person parameters..... 23

 5.2.3 Test targeting and reliability 23

 5.3 Quality of the Test 25

 5.3.1 Item fit..... 25

 5.3.2 Differential item functioning..... 25

 5.3.3 Rasch homogeneity..... 31

6 Discussion..... 31

7 Data in the Scientific Use File..... 32

References..... 33

Appendix 36

1 Introduction

In the National Educational Panel Study (NEPS) different competences are measured coherently across the life span. Tests have been developed for different competence domains. These include, among other things, reading competence, mathematical competence, scientific literacy, information and communication technologies literacy, metacognition, vocabulary, and domain-general cognitive functioning.

Most of the competence data are scaled with models that are based on item response theory (IRT). Because most of the competence tests were developed specifically for implementation in NEPS, several analyses have been conducted to evaluate the quality of the tests. The IRT models chosen to scale the competence data and the analyses performed to check the quality of the scales are described in Pohl and Carstensen (2012).

This paper presents the results of the physics competence test in two waves of the additional study Thuringia. In this study, items were composed for the physics competence test used across two consecutive school years (2009/10 and 2010/11) to test secondary-school students' physics competences in their final year of Gymnasium (the type of school that leads to upper secondary education and the Abitur). More detailed information about the aims of this study as well as further information about the test can be found on the NEPS website¹.

The present report draws strongly on previous technical reports such as Hübner, Rieger, and Wagner (2016), Pohl, Haberkorn, Hardt, and Wiegand (2012) and Pohl and Carstensen (2012). It includes extracts from these previous reports.

2 Testing Physics Competence

The framework and item development is corresponded to the Thuringian curriculum for physics (Thüringer Kultusministerium, 1999). Furthermore, it takes the basic requirements for the Abitur in physics into account (Einheitliche Prüfungsanforderungen für die Abiturprüfung in Physik; KMK, 2004). The items of the physics competence test are composed of a few different studies (some of the items are unpublished). Table 1 depicts the sources where the items were obtained.

1 <https://www.neps-data.de/en-us/datacenter/dataanddocumentation/additionalstudythuringia.aspx>

Table 1

Source of Items in the Physics Competence Test

| Source | Frequency |
|---|------------------|
| TIMSS II | 3 |
| TIMSS III | 24 |
| Thermodynamik Testinventar ¹ | 10 |
| BEMA ² | 4 |
| Proprietary development ³ | 23 |
| Total number of items | 64 |

References: ¹Einhaus, 2007; ²Ding, Chabay, Sherwood, & Beichner, 2006; ³Viering & Neumann, 2008; TIMSS II, 1995; TIMSS III, 1995

In the following, we will point out specific aspects of the physics competence paper-and-pencil test that are necessary for understanding the scaling results presented in this paper. The items are not arranged in units. Thus, on the test, students must usually read a certain situation and must subsequently answer only one task related to it.

There are three types of response formats in the physics competence test. These are simple multiple choice (MC), complex multiple choice (CMC), and short constructed response (SCR). For MC items, the test taker has to choose the correct answer out of several - usually four or five- response options. For CMC tasks, a number of subtasks with three response options are presented. SCR items require the test taker to fill in an answer into an empty field. Tables 2 and 3 show how the content areas and response formats are distributed across the items as well as booklets (for the content area of each item see Table S2 in the Appendix D).

Table 2

Content Areas of the Items on the Physics Competence Test

| Content area | Frequency |
|---|------------------|
| Electrical fields and interdependency | 6 |
| Magnetic fields and electromagnetic induction | 12 |
| Waves | 8 |
| Optics | 8 |
| Quantum physics: Quanta and matter | 5 |
| Dynamics: Mechanics of the Rigid Body | 7 |
| Thermodynamics | 16 |
| Special Theory of Relativity | 2 |
| Total number of items | 64 |

| Number of Items by Content Area and Booklet | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| Electrical fields and interdependency | 2 | 2 | 3 | 2 | 2 | 2 | 2 | 1 | 2 |
| Magnetic fields and electromagnetic induction | 2 | 3 | 5 | 3 | 2 | 3 | 4 | 5 | 4 |
| Waves | 4 | 3 | 1 | 2 | 3 | 3 | 3 | 2 | 2 |
| Optics | 2 | 2 | 2 | 2 | 3 | 3 | 3 | 3 | 3 |
| Quantum physics: Quanta and matter | 1 | 1 | 1 | 1 | 1 | 2 | 2 | 1 | - |
| Dynamics: Mechanics of the Rigid Body | 1 | 2 | 2 | 2 | 2 | 1 | 1 | 2 | 1 |
| Thermodynamics | 5 | 3 | 4 | 8 | 10 | 6 | 3 | 2 | 4 |
| Special Theory of Relativity | 1 | 1 | - | - | - | - | - | 1 | 1 |
| Total number of items | 18 | 17 | 18 | 20 | 23 | 20 | 18 | 17 | 17 |

Table 3

Response Formats of the Items on the Physics Competence Test

| Response format | Frequency |
|------------------------------|------------------|
| Single multiple choice | 51 |
| Complex multiple choice | 7 |
| Short constructed response | 6 |
| Total number of items | 64 |

| Number of Items by Response For- mat and Booklet | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|---|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Single multiple choice | 17 | 18 | 18 | 17 | 16 | 17 | 18 | 12 | 12 |
| Complex multiple choice | - | - | - | 4 | 7 | 3 | - | - | - |
| Short constructed response | 1 | - | - | - | - | - | - | 5 | 5 |
| Total number of items | 18 | 18 | 18 | 21 | 23 | 20 | 18 | 17 | 17 |

3 Data

A description of the design of the study, the sample, as well as the instruments that were used can be found on the NEPS website². A total of 2,254 participants took the physics competence test: 1,370 in 2009/2010 (Wave 1), and 884 in 2010/2011 (Wave 2)³. All subjects gave at least one valid answer so that for every subject, a competence score was estimated.

4 Analyses

This section briefly describes the analyses that were computed; these included inspecting the various missing responses, scaling the data, and examining the psychometric quality of the test.

4.1 Missing Responses

There are different types of missing responses in competence test data. These include (among others) missing responses due to a) invalid responses, b) omitted items, c) items that test takers did not reach, and d) items that are missing by design (e.g., due to the different booklets). Missing responses provide information about how well the test worked (e.g., time limits, whether participants understood the instructions, how participants handled different response formats), and they need to be accounted for in the estimation of item and person parameters. We thoroughly inspected the occurrence of missing responses per person. This provided an indication of how well the test takers coped with the test. We then examined the occurrence of missing responses per item in order to obtain some information about how well the items performed. In addition, information was available about whether students did not take the physics competence test (e.g., due to student tardiness) but did take at least one of the other competence tests (mathematics, or biology). This missing code is referred to as e) missing by non-participation.

4.2 Scaling Model

In order to estimate the item and person parameters for physics competence, a Rasch model (Rasch, 1960) was used and estimated in ConQuest 4.2 (Wu, Adams, Wilson, & Haldane, 2007).

Item parameters are estimated difficulties for dichotomous variables in the Rasch model. Ability estimates for physics competence were estimated as weighted maximum likelihood estimates (WLEs; Warm, 1989). Person parameter estimation in NEPS is described by Pohl and Carstensen (2012), whereas the data available in the SUF are described in Section 7.

Plotting the item parameters in relation to the ability estimates of the persons was used in order to judge how well the item difficulties were targeted toward the test persons' abilities (see Figure 5). The test targeting provides some information about the precision of the ability estimates at different levels of ability.

2 <https://www.neps-data.de/en-us/datacenter/dataanddocumentation/additionalstudythuringia/documentation.aspx>

3 The dataset contains 2,260 persons.

4.3 Checking the Quality of the Scale

To ensure that the test featured appropriate psychometric properties, the quality of the test was examined with several analyses.

The item fit of dichotomous items was examined by analyzing them via a Rasch model (Rasch, 1960). We examined the weighted (or “infit”) mean square (WMNSQ), the respective t-value, and correlations between the item score and the total score. In accordance with Pohl and Carstensen (2012), items with a WMNSQ > 1.15 (t-value > |6|) were considered to have a noticeable item misfit, and items with a WMNSQ > 1.20 (t-value > |8|) were considered to have a considerable item misfit, and their performance was further investigated. Correlations between an item score and the total score (equal to the discrimination as computed in ConQuest) greater than 0.3 were considered good, greater than 0.2 acceptable, and below 0.2 problematic. Overall, the judgment of item fit was based on all fit indicators.

Our aim was to construct a physics competence test that measured the same construct in all participants. If any items favored a certain subgroup (e.g., items that were easier for males than for females), measurement invariance would be violated, and a comparison of competence scores between the subgroups (e.g., males and females) would be biased and, thus, unfair.⁴ We addressed the issue of measurement invariance by investigating test fairness for the variables gender, books at home (as a proxy for socioeconomic status; see Pohl and Carstensen, 2012 for a description of these variables), and wave (i.e., to which of the two waves do subjects belong?). Differential item functioning (DIF) was estimated by applying a multifaceted IRT model in ConQuest, in which the main effects of the subgroups and the differential effects of the subgroups on item difficulty were modeled. Differences in the estimated item difficulties between the subgroups were evaluated. On the basis of our experiences with the preliminary data (e.g., Pohl & Carstensen, 2012), we judged absolute differences in estimated difficulties that were greater than 1 logit as having very strong DIF, absolute differences between 0.6 and 1 as worthy of further investigation, differences between 0.4 and 0.6 as considerable but not significant, and differences smaller than 0.4 as not having any considerable DIF. In addition to computing DIF analyses at the item level, we investigated test fairness by comparing a model that included differential item functioning with a model that estimated only main effects but no DIF.

The physics competence data were scaled with the Rasch model, which assumes Rasch homogeneity. Nonetheless, Rasch homogeneity is an assumption that might not hold for empirical data. We therefore checked for deviations from uniform discrimination. We estimated item discrimination by applying the Birnbaum model (2PL; Birnbaum, 1968) with the TAM package in R (Robitzsch, Kiefer, & Wu, 2017; R Core Team, 2017).

⁴ It should be noted that differential item functioning may also reflect valid differences between subgroups – that is, item impact (Zumbo, 1999).

5 Results

In this section, the key scaling results of the two waves of the additional study Thuringia will be presented.

5.1 Missing Responses

In this subsection, we first report the number of missing responses that can be categorized into the different types of missing responses as described in Chapter 4.1 per person and the total number of missing responses per person. Afterwards, we describe the missing responses per item.

5.1.1 Missing responses per person

Figure 1 shows the number of *invalid responses* per person. As can be seen, 5.75% of the participants produced any invalid responses. The maximum number of invalid responses was 6.

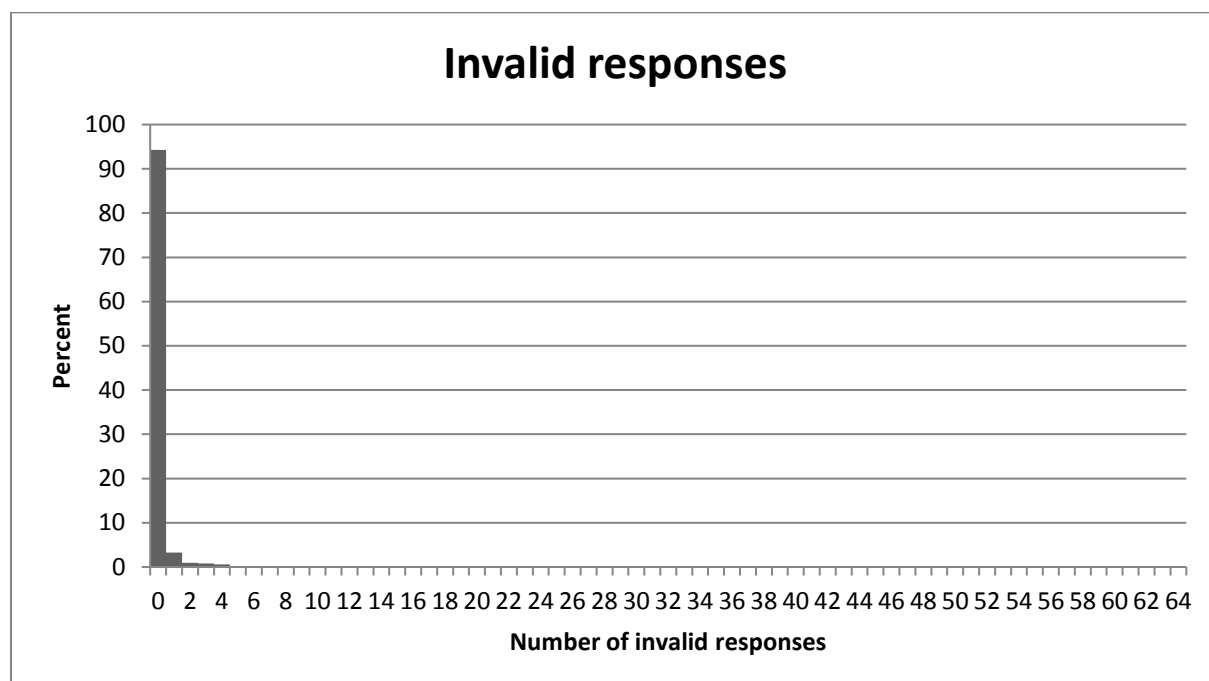


Figure 1. Number of invalid responses per person.

The largest source of missing responses on this test was the *omission of items*. As can be seen in Figure 2, almost one out of four of the participants (22.54%) skipped at least one item. Overall, 3.15% of the participants omitted five or more items.

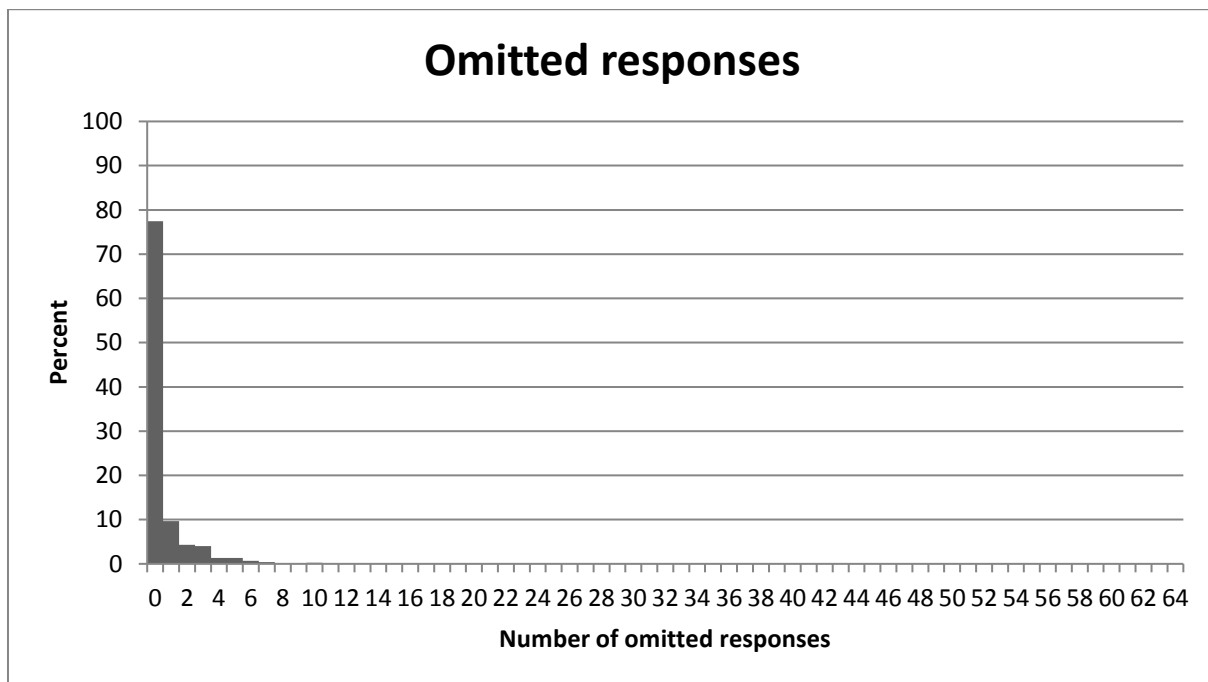


Figure 2. Number of omitted responses per person.

By definition, every item after the last item that was completed is labeled *not reached*. As Figure 3 shows, most participants (89.16%) reached the end of the test. Only 1.22% did not reach the fifth last item.

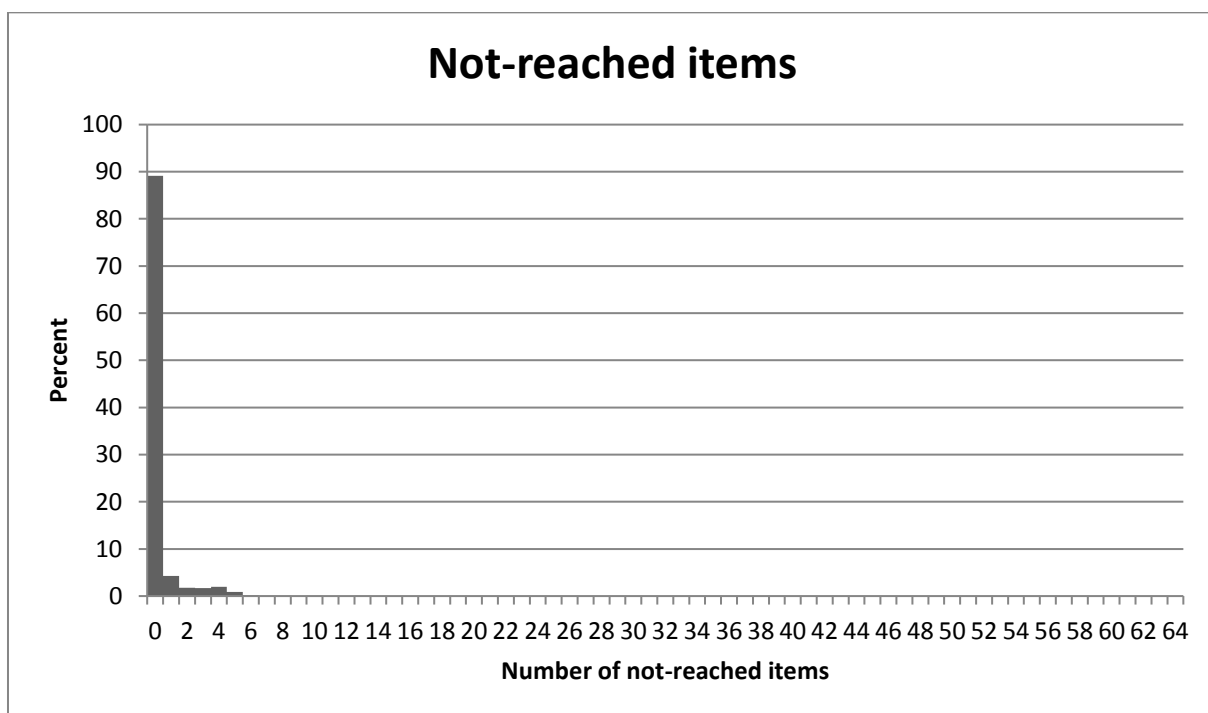


Figure 3. Number of not-reached items per person.

Overall, 89.16% of the participants had no items that were missing by *non-participation*. Only 0.27% of the students did not take the physics competence test but did take at least one of the other tests.

The total number of missing responses (excluding those missing by non-participation and missing by design) aggregated across the invalid, omitted, and not-reached missing responses per person is illustrated in Figure 4. On average, the participants produced 0.95 (SD = 1.97) missing responses. Moreover, 68.27% of the persons had no missing response at all. Only 5.00% of the participants had five or more missing responses.

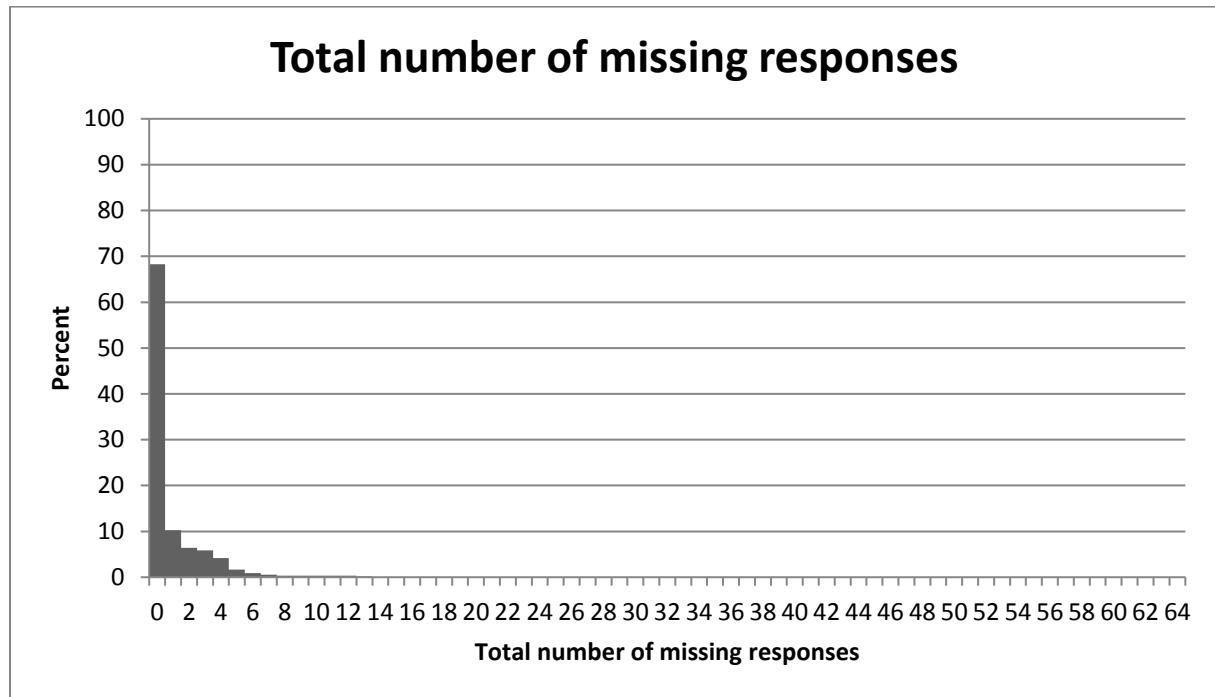


Figure 4. Total number of missing responses.

5.1.2 Missing responses per item

Table 4 provides information about the occurrence of the different kinds of responses that were missing per item. A maximum of 6.3% of the participants failed to reach items (column 5). None of the 64 items had an omission rate that exceeded 5% (column 6). Overall, the percentage of invalid responses per item (column 7) was very low (the maximum was 1.7% for item *phyn9t_c*). The percentage of items that were missing by non-participation (column 8) was very low (the maximum was 0.3%). The percentage of missing by designs per items is displayed in column 8. The percentages ranged from 76.8% to 81.2%.

5.2 Parameter Estimates

5.2.1 Item parameters

The second column in Table 5 shows the percentage of correct responses relative to all valid responses for each item. Please note that, because there is a nonnegligible number of missing responses, this probability cannot be interpreted as an index of item difficulty. The percentage of correct responses varied from 9.6% to 88.2% with an average of 38.57 % (SD = 20.02%) correct responses.

For reasons of model identification, in the Rasch model, the mean of the ability distribution was constrained to be zero. The estimated item difficulties (for dichotomous variables) are given in the third column of Table 5. The item difficulties ranged from -2.187 (item phyr1_c) to 2.627 (item phyn2t_c) logits with an average difficulty of 0.64 logits ($SD = 1.10$). Altogether, the item difficulties were somewhat high. The 2PL discrimination parameters ranged from 0.040 to 3.695 (see again Table 5). The items phye6_c, phyt13b_c, phyt13c_c, phyg13_c, phyb18_c, phyn2_c, and phyt9_c had a negative discrimination, paradoxically indicating that students with lower ability had a higher probability of solving the item. Therefore, after we rechecked the coding procedure, those items were excluded from further analyses (see Table S1 in Appendix C).

Table 4

Missing Values

| | Item | Booklet | Position in the test | Number of valid responses | Percentage of not-reached responses | Percentage of omitted responses | Percentage of invalid responses | Percentage of missing by non-participation | Percentage of missing by design |
|----|----------|---------|----------------------|---------------------------|-------------------------------------|---------------------------------|---------------------------------|--|---------------------------------|
| 1 | phyh10_c | 1-9 | 1 | 2210 | - | 1.7 | 0.2 | 0.3 | - |
| 2 | phyg1_c | 1-9 | 2 | 2198 | - | 2.5 | - | 0.3 | - |
| 3 | phyn5_c | 1-9 | 3 | 2168 | - | 3.7 | 0.1 | 0.3 | - |
| 4 | phyr1_c | 1-9 | 4 | 2248 | - | 0.2 | 0.0 | 0.3 | - |
| 5 | phyg2_c | 1-9 | 5 | 2212 | 0.0 | 0.5 | 1.3 | 0.3 | - |
| 6 | phye2_c | 1-9 | 6 | 2196 | 0.0 | 2.5 | - | 0.3 | - |
| 7 | phyh8_c | 1,9 | 7/12 | 510 | - | 0.3 | 0.1 | 0.3 | 76.8 |
| 8 | phyn1_c | 1,9 | 8/13 | 508 | - | 0.4 | 0.0 | 0.3 | 76.8 |
| 9 | phyg8_c | 1,9 | 9/14 | 505 | 0.0 | 0.5 | 0.0 | 0.3 | 76.8 |
| 10 | phym14_c | 1,9 | 10/15 | 506 | - | 0.4 | 0.1 | 0.3 | 76.8 |
| 11 | phyt1_c | 1,9 | 11/16 | 513 | 0.1 | 0.1 | 0.0 | 0.3 | 76.8 |
| 12 | phyg6_c | 1,9 | 12/17 | 496 | 0.6 | 0.3 | 0.1 | 0.3 | 76.8 |
| 13 | phyh12_c | 1,2 | 13/7 | 473 | - | 1.1 | 0.1 | 0.3 | 77.6 |
| 14 | phyn12_c | 1,2 | 14/8 | 487 | 0.0 | 0.5 | - | 0.3 | 77.6 |

| | Item | Booklet | Position in the test | Number of valid responses | Percentage of not-reached responses | Percentage of omitted responses | Percentage of invalid responses | Percentage of missing by non-participation | Percentage of missing by design |
|----|----------|---------|----------------------|---------------------------|-------------------------------------|---------------------------------|---------------------------------|--|---------------------------------|
| 15 | phyh2_c | 1,2 | 15/9 | 490 | 0.1 | 0.2 | 0.2 | 0.3 | 77.6 |
| 16 | phyh5_c | 1,2 | 16/10 | 477 | 0.1 | 0.9 | - | 0.3 | 77.6 |
| 17 | phyn7_c | 1,2 | 17/11 | 487 | 0.1 | 0.4 | 0.1 | 0.3 | 77.6 |
| 18 | phyf3_c | 1,2 | 18/12 | 473 | 0.4 | 0.7 | 0.0 | 0.3 | 77.6 |
| 19 | phyb6_c | 2,3 | 13/7 | 482 | - | 0.5 | 0.1 | 0.3 | 77.7 |
| 20 | phyg4_c | 2,3 | 14/8 | 487 | - | 0.4 | - | 0.3 | 77.7 |
| 21 | phyn4_c | 2,3 | 15/9 | 472 | - | 1.1 | 0.0 | 0.3 | 77.7 |
| 22 | phyn10_c | 2,3 | 16/10 | 488 | - | 0.4 | - | 0.3 | 77.7 |
| 23 | phyf5_c | 2,3 | 17/11 | 496 | - | 0.0 | - | 0.3 | 77.7 |
| 24 | phyn13_c | 2,3 | 18/12 | 486 | 0.2 | 0.3 | 0.0 | 0.3 | 77.7 |
| 25 | phyb14_c | 3,4 | 13/7 | 448 | 0.0 | 2.1 | 0.1 | 0.3 | 77.7 |
| 26 | phyh6_c | 3,4 | 14/8 | 476 | 0.0 | 0.9 | 0.0 | 0.3 | 77.7 |
| 27 | phyn6_c | 3,4 | 15/9 | 456 | 0.0 | 0.4 | 0.2 | 0.3 | 77.7 |
| 28 | phyn15_c | 3,4 | 16/10 | 485 | 0.0 | 0.4 | 0.2 | 0.3 | 77.7 |
| 29 | phyt3_c | 3,4 | 17/11 | 486 | 0.1 | 0.4 | 0.0 | 0.3 | 77.7 |
| 30 | phyf1_c | 3,4 | 18/12 | 466 | 0.4 | 0.8 | 0.2 | 0.3 | 77.7 |

| | Item | Booklet | Position in the test | Number of valid responses | Percentage of not-reached responses | Percentage of omitted responses | Percentage of invalid responses | Percentage of missing by non-participation | Percentage of missing by design |
|----|-----------|---------|----------------------|---------------------------|-------------------------------------|---------------------------------|---------------------------------|--|---------------------------------|
| 31 | phye6_c | 4,5 | 13/7 | 474 | - | 1.0 | 0.0 | 0.3 | 77.7 |
| 32 | phye1_c | 4,5 | 14/8 | 492 | - | 0.1 | 0.1 | 0.3 | 77.7 |
| 33 | phyn9_c | 4,5 | 15/9 | 447 | - | 2.2 | - | 0.3 | 77.7 |
| 34 | phyo13_c | 4,5 | 16/10 | 497 | - | - | - | 0.3 | 77.7 |
| 35 | phyt13a_c | 4,5 | 17/11 | 456 | 0.6 | 1.2 | - | 0.3 | 77.7 |
| 36 | phyt13b_c | 4,5 | 18/12 | 459 | 0.6 | 1.1 | - | 0.3 | 77.7 |
| 37 | phyt13c_c | 4,5 | 19/13 | 452 | 0.6 | 1.3 | 0.0 | 0.3 | 77.7 |
| 38 | phyt13d_c | 4,5 | 20/14 | 457 | 0.6 | 1.2 | - | 0.3 | 77.7 |
| 39 | phyf9_c | 4,5 | 21/15 | 448 | 1.2 | 0.7 | 0.2 | 0.3 | 77.7 |
| 40 | phyf6_c | 5,6 | 16/7 | 475 | - | 0.9 | 0.0 | 0.3 | 77.8 |
| 41 | phyg13_c | 5,6 | 17/8 | 493 | - | 0.1 | - | 0.3 | 77.8 |
| 42 | phyn8_c | 5,6 | 18/9 | 482 | 0.0 | 0.4 | 0.1 | 0.3 | 77.8 |
| 43 | phyn14_c | 5,6 | 19/10 | 483 | 0.1 | 0.4 | 0.1 | 0.3 | 77.8 |
| 44 | phyt4a_c | 5,6 | 20/11 | 471 | 0.1 | 1.0 | - | 0.3 | 77.8 |
| 45 | phyt4b_c | 5,6 | 21/12 | 467 | 0.1 | 1.2 | - | 0.3 | 77.8 |
| 46 | phyt4c_c | 5,6 | 22/13 | 477 | 0.2 | 0.6 | 0.0 | 0.3 | 77.8 |

| | Item | Booklet | Position in the test | Number of valid responses | Percentage of not-reached responses | Percentage of omitted responses | Percentage of invalid responses | Percentage of missing by non-participation | Percentage of missing by design |
|----|-----------|---------|----------------------|---------------------------|-------------------------------------|---------------------------------|---------------------------------|--|---------------------------------|
| 47 | phyf7_c | 5,6 | 23/14 | 471 | 0.4 | 0.5 | 0.2 | 0.3 | 77.8 |
| 48 | phyb18_c | 6,7 | 15/7 | 462 | - | 0.9 | - | 0.3 | 78.4 |
| 49 | phyn3_c | 6,7 | 16/8 | 477 | - | 0.3 | - | 0.3 | 78.4 |
| 50 | phyn2_c | 6,7 | 17/9 | 443 | - | 1.8 | - | 0.3 | 78.4 |
| 51 | phyg5_c | 6,7 | 18/10 | 478 | - | 0.1 | 0.1 | 0.3 | 78.4 |
| 52 | phyt9_c | 6,7 | 19/11 | 468 | 0.1 | 0.5 | 0.1 | 0.3 | 78.4 |
| 53 | phyh3_c | 6,7 | 20/12 | 465 | 0.4 | 0.3 | 0.0 | 0.3 | 78.4 |
| 54 | phyb24_c | 7,8 | 13/7 | 475 | 0.1 | 0.6 | 0.2 | 0.3 | 77.8 |
| 55 | phyg19_c | 7,8 | 14/8 | 489 | 0.1 | 0.0 | 0.1 | 0.3 | 77.8 |
| 56 | phyf13_c | 7,8 | 15/9 | 479 | 0.1 | 0.6 | - | 0.3 | 77.8 |
| 57 | phyn11_c | 7,8 | 16/10 | 483 | 0.1 | 0.2 | 0.3 | 0.3 | 77.8 |
| 58 | phyf4_c | 7,8 | 17/11 | 475 | 0.4 | 0.6 | - | 0.3 | 77.8 |
| 59 | phyh15_c | 7,8 | 18/12 | 444 | 1.1 | 1.2 | - | 0.3 | 77.8 |
| 60 | phyn12t_c | 8,9 | 13/7 | 491 | 0.4 | 0.3 | 0.0 | 0.3 | 77.3 |
| 61 | phyh5t_c | 8,9 | 14/8 | 354 | 2.3 | 1.6 | 0.7 | 0.3 | 79.5 |
| 62 | phyh6t_c | 8,9 | 15/9 | 243 | 3.8 | 2.3 | 1.6 | 0.3 | 81.2 |

| | Item | Booklet | Position in the test | Number of valid responses | Percentage of not-reached responses | Percentage of omitted responses | Percentage of invalid responses | Percentage of missing by non-participation | Percentage of missing by design |
|----|----------|---------|----------------------|---------------------------|-------------------------------------|---------------------------------|---------------------------------|--|---------------------------------|
| 63 | phyn9t_c | 8,9 | 16/10 | 212 | 5.2 | 2.5 | 1.7 | 0.3 | 81.0 |
| 64 | phyn2t_c | 8,9 | 17/11 | 189 | 6.3 | 2.3 | 1.6 | 0.3 | 81.2 |

Table 5

Item Parameters of the Physics Competence Test

| | Item | Percentage correct | Difficulty/ location parameter | SE (difficulty/ location parameter) | WMNSQ | WMNSQ t-value | Correlation of item score with total score | Discrimination-2 PL |
|---|----------|--------------------|--------------------------------|-------------------------------------|-------|---------------|--|---------------------|
| 1 | phyh10_c | 16.22 | 1.799 | 0.062 | 0.97 | -0.7 | 0.36 | 1.115 |
| 2 | phyg1_c | 35.31 | 0.666 | 0.049 | 1.07 | 3.9 | 0.26 | 0.318 |
| 3 | phyn5_c | 42.96 | 0.311 | 0.048 | 0.94 | -4.5 | 0.50 | 1.632 |
| 4 | phyr1_c | 88.20 | -2.187 | 0.069 | 0.97 | -0.7 | 0.32 | 1.523 |
| 5 | phyg2_c | 60.93 | -0.494 | 0.048 | 0.98 | -1.1 | 0.43 | 1.145 |
| 6 | phye2_c | 60.47 | -0.477 | 0.048 | 1.00 | 0.3 | 0.37 | 0.832 |
| 7 | phyh8_c | 12.97 | 2.081 | 0.140 | 0.98 | -0.2 | 0.37 | 1.093 |
| 8 | phyn1_c | 28.80 | 0.965 | 0.107 | 1.05 | 1.1 | 0.30 | 0.478 |
| 9 | phyg8_c | 24.40 | 1.230 | 0.113 | 0.90 | -1.8 | 0.54 | 1.890 |

| Item | Percentage correct | Difficulty/ location parameter | SE (difficulty/ location parameter) | WMNSQ | WMNSQ t-value | Correlation of item score with total score | Discrimination-2 PL | |
|------|--------------------|--------------------------------|-------------------------------------|-------|---------------|--|---------------------|-------|
| 10 | phym14_c | 82.18 | -1.730 | 0.124 | 1.02 | 0.2 | 0.28 | 0.612 |
| 11 | phyt1_c | 39.45 | 0.436 | 0.099 | 0.98 | -0.6 | 0.45 | 1.130 |
| 12 | phyg6_c | 64.24 | -0.701 | 0.103 | 1.00 | -0.0 | 0.38 | 0.824 |
| 13 | phyh12_c | 16.49 | 1.743 | 0.132 | 0.97 | -0.3 | 0.40 | 1.307 |
| 14 | phyn12_c | 26.90 | 1.069 | 0.110 | 0.97 | -0.6 | 0.42 | 1.109 |
| 15 | phyh2_c | 38.78 | 0.464 | 0.101 | 1.01 | 0.2 | 0.39 | 0.807 |
| 16 | phyh5_c | 39.83 | 0.412 | 0.102 | 1.01 | 0.4 | 0.38 | 0.787 |
| 17 | phyn7_c | 39.63 | 0.430 | 0.101 | 0.98 | -0.6 | 0.46 | 1.078 |
| 18 | phyf3_c | 34.46 | 0.676 | 0.105 | 1.05 | 1.2 | 0.30 | 0.466 |
| 19 | phyb6_c | 16.60 | 1.774 | 0.129 | 1.00 | -0.0 | 0.35 | 0.925 |
| 20 | phyg4_c | 33.06 | 0.792 | 0.104 | 1.09 | 2.3 | 0.19 | 0.040 |
| 21 | phyn4_c | 11.44 | 2.234 | 0.151 | 1.02 | 0.2 | 0.20 | 0.423 |
| 22 | phyn10_c | 28.89 | 1.008 | 0.107 | 1.01 | 0.1 | 0.36 | 0.886 |
| 23 | phyf5_c | 46.57 | 0.166 | 0.098 | 1.00 | 0.1 | 0.39 | 0.812 |
| 24 | phyn13_c | 35.60 | 0.667 | 0.102 | 1.09 | 2.4 | 0.21 | 0.070 |
| 25 | phyb14_c | 9.62 | 2.430 | 0.166 | 1.03 | 0.3 | 0.10 | 0.120 |
| 26 | phyh6_c | 35.79 | 0.683 | 0.103 | 1.08 | 2.3 | 0.21 | 0.084 |

| Item | Percentage correct | Difficulty/ location parameter | SE (difficulty/ location parameter) | WMNSQ | WMNSQ t-value | Correlation of item score with total score | Discrimination-2 PL |
|--------------|--------------------|--------------------------------|-------------------------------------|-------|---------------|--|---------------------|
| 27 phyn6_c | 37.80 | 0.588 | 0.104 | 1.02 | 0.5 | 0.34 | 0.703 |
| 28 phyn15_c | 24.17 | 1.278 | 0.113 | 1.03 | 0.6 | 0.29 | 0.433 |
| 29 phyt3_c | 31.55 | 0.884 | 0.105 | 1.02 | 0.5 | 0.27 | 0.442 |
| 30 phyf1_c | 51.18 | -0.009 | 0.100 | 1.06 | 2.1 | 0.28 | 0.117 |
| 31 phye6_c | - | - | - | - | - | - | - |
| 32 phye1_c | 79.84 | -1.486 | 0.119 | 1.04 | 0.6 | 0.25 | 0.575 |
| 33 phyn9_c | 50.67 | -0.033 | 0.103 | 1.08 | 2.9 | 0.26 | 0.214 |
| 34 phyo13_c | 77.82 | -1.355 | 0.115 | 1.04 | 0.7 | 0.25 | 0.401 |
| 35 phyt13a_c | 81.76 | -1.633 | 0.128 | 1.07 | 0.9 | 0.16 | 0.156 |
| 36 phyt13b_c | - | - | - | - | - | - | - |
| 37 phyt13c_c | - | - | - | - | - | - | - |
| 38 phyt13d_c | 40.79 | 0.390 | 0.103 | 1.04 | 1.2 | 0.32 | 0.476 |
| 39 phyf9_c | 19.69 | 1.515 | 0.126 | 0.99 | -0.1 | 0.33 | 0.855 |
| 40 phyf6_c | 18.11 | 1.630 | 0.126 | 0.97 | -0.4 | 0.37 | 0.902 |
| 41 phyg13_c | - | - | - | - | - | - | - |
| 42 phyn8_c | 21.58 | 1.400 | 0.118 | 0.92 | -1.3 | 0.47 | 1.777 |
| 43 phyn14_c | 33.75 | 0.731 | 0.104 | 0.96 | -1.0 | 0.43 | 1.103 |

| Item | Percentage correct | Difficulty/ location parameter | SE (difficulty/ location parameter) | WMNSQ | WMNSQ t-value | Correlation of item score with total score | Discrimination-2 PL | |
|------|--------------------|--------------------------------|-------------------------------------|-------|---------------|--|---------------------|-------|
| 44 | phyt4a_c | 74.95 | -1.206 | 0.114 | 1.01 | 0.2 | 0.34 | 0.577 |
| 45 | phyt4b_c | 62.96 | -0.593 | 0.104 | 1.03 | 0.9 | 0.32 | 0.526 |
| 46 | phyt4c_c | 22.43 | 1.356 | 0.117 | 1.05 | 0.9 | 0.21 | 0.254 |
| 47 | phyf7_c | 36.31 | 0.601 | 0.104 | 1.04 | 1.2 | 0.29 | 0.412 |
| 48 | phyb18_c | - | - | - | - | - | - | - |
| 49 | phyn3_c | 56.09 | -0.280 | 0.101 | 0.96 | -1.3 | 0.48 | 1.283 |
| 50 | phyn2_c | - | - | - | - | - | - | - |
| 51 | phyg5_c | 33.33 | 0.763 | 0.105 | 1.00 | 0.0 | 0.42 | 0.890 |
| 52 | phyt9_c | - | - | - | - | - | - | - |
| 53 | phyh3_c | 36.42 | 0.610 | 0.105 | 0.99 | -0.2 | 0.43 | 0.971 |
| 54 | phyb24_c | 14.98 | 1.921 | 0.137 | 1.04 | 0.5 | 0.28 | 0.704 |
| 55 | phyg19_c | 47.54 | 0.112 | 0.100 | 0.98 | -0.8 | 0.46 | 1.024 |
| 56 | phyf13_c | 50.42 | -0.026 | 0.101 | 0.93 | -2.5 | 0.53 | 1.540 |
| 57 | phyn11_c | 34.23 | 0.721 | 0.105 | 0.96 | -1.1 | 0.48 | 1.317 |
| 58 | phyf4_c | 24.47 | 1.252 | 0.116 | 0.97 | -0.6 | 0.47 | 1.365 |
| 59 | phyh15_c | 30.93 | 0.875 | 0.112 | 1.10 | 2.2 | 0.22 | 0.200 |
| 60 | phyn12t_c | 14.69 | 0.610 | 0.105 | 0.99 | -0.2 | 0.49 | 1.759 |

| Item | Percentage correct | Difficulty/ location parameter | SE (difficulty/ location parameter) | WMNSQ | WMNSQ t-value | Correlation of item score with total score | Discrimination-2 PL |
|-------------|--------------------|--------------------------------|-------------------------------------|-------|---------------|--|---------------------|
| 61 phyh5t_c | 20.40 | 1.972 | 0.136 | 0.93 | -0.8 | 0.61 | 2.616 |
| 62 phyh6t_c | 27.69 | 1.585 | 0.143 | 0.87 | -1.7 | 0.49 | 1.384 |
| 63 phyn9t_c | 10.43 | 1.270 | 0.157 | 0.95 | -0.7 | 0.45 | 1.663 |
| 64 phyn2t_c | 12.77 | 2.627 | 0.238 | 0.97 | -0.1 | 0.62 | 3.695 |

Note. Difficulty = Item difficulty / location parameter, SE = Standard error of item difficulty / location parameter, WMNSQ = Weighted mean square, t = t-value for WMNSQ. Items 31, 36, 37, 41, 48, 50, and 52 were excluded from the analyses due to an unsatisfactory item fit.

5.2.2 Person parameters

The person parameters were estimated as WLEs (Pohl & Carstensen, 2012). A description of the data in the SUF can be found in Section 7. An overview of how to work with competence data is presented by Pohl and Carstensen (2012).

5.2.3 Test targeting and reliability

Test targeting focuses on how well item difficulties and person abilities are matched; this is an important criterion for evaluating the appropriateness of the test for the target group. In Figure 5, the item difficulties and person abilities are plotted on the same scale. The items covered rather the medium and higher part of the ability distribution well but, in general, items were somewhat difficult. Hence, the test can measure person abilities in the medium and high-ability regions relatively precisely, whereas low person abilities are measured with larger standard errors of measurement.

The mean of the ability distribution was constrained to be zero, and its variance was estimated to be 0.497⁵, indicating a reasonable differentiation between the subjects. The reliability of the test (EAP/PV reliability = .58, WLE reliability = .55) was modest. This should be related to the suboptimal test targeting described above.

5 Seven items (i.e., phye6_c, phyt13b_c, phyt13c_c, phyg13_c, phyb18_c, phyn2_c, and phyt9_c) were excluded due to negative item discriminations (see also Section 5.2.1).

| Scale (in logits) | Person ability | Item difficulty |
|-------------------|--|------------------|
| | | 56 |
| | X | |
| | | 24 |
| | | 57 |
| | | 20 |
| | | 7 |
| 2 | X | |
| | XXX | 46 53 |
| | X | 1 |
| | X | 12 18 |
| | XXX | 36 |
| | XXX | 35 54 |
| | XXXXXX | |
| | XXXXXXXX | 37 41 |
| | XXXXXX | 9 27 50 55 |
| | XXXXXXXX | |
| | XXXXXXXX | 13 |
| 1 | XXXXXXXXXXXX | 8 21 |
| | XXXXXXXXXXXXXXXX | 28 51 |
| | XXXXXXXXXXXXXXXX | 19 44 |
| | XXXXXXXXXXXXXXXXXXXX | 2 17 23 25 38 49 |
| | XXXXXXXXXXXXXXXXXXXX | 26 42 45 |
| | XXXXXXXXXXXXXXXXXXXX | |
| | XXXXXXXXXXXXXXXXXXXX | 10 14 15 16 34 |
| | XXXXXXXXXXXXXXXXXXXX | 3 |
| | XXXXXXXXXXXXXXXXXXXX | |
| 0 | XX | 22 47 |
| | XX | |
| | XX | 29 31 48 |
| | XX | |
| | XX | 43 |
| | XX | |
| | XX | |
| | XX | 5 6 |
| | XX | 40 |
| | XXXXXXXXXXXXXXXXXXXX | 11 |
| | XXXXXXXXXXXXXXXXXXXX | |
| | XXXXXXXXXXXXXXXXXXXX | |
| | XXXXXXXXXXXX | |
| | XXXXXXXX | 39 |
| | XXXX | |
| | XXX | 32 |
| | XXX | 30 |
| | XX | |
| | XXX | 33 |
| | X | 52 |
| | X | |
| | X | |
| -2 | | 4 |

Figure 5. Test targeting. The distribution of person abilities in the sample is depicted on the left-hand side, with each 'X' representing 3.8 cases. The item difficulties (or location parameters) are depicted on the right-hand side. Each number represents one item with a corresponding position in the test, cf. Table 4.

5.3 Quality of the Test

5.3.1 Item fit

Altogether, the item fit could be considered moderate, with values of the WMNSQ ranging from 0.90 (item phyg8_c) to 1.10 (item phyh15_c), cf. column 5 of Table 5. Point-biserial correlations between the item scores and the total scores ranged from 0.10 (items phyb14_c and phyb18_c) to 0.62 (item phyn2t_c). Discriminations estimated in the 2PL-model with the TAM package in R ranged from 0.040 (item phyg4_c) to 3.695 (item phyn2t_c), cf. Table 5, column 8.

5.3.2 Differential item functioning

Differential item functioning (DIF) was used to evaluate test fairness for several subgroups (i. e., measurement invariance). For this purpose, DIF was examined for the variables gender, books, and wave (see Pohl & Carstensen, 2012, for a description of these variables). Table 6 provides a summary of the results of the DIF analyses. According to Pohl and Carstensen (2012), absolute difficulty differences greater than 1 logit can be considered to show very strong DIF. For the current test, four items exceeded this threshold.

The table depicts the differences in the estimated item difficulties between the respective groups. “Male vs. female”, for example, indicates the difference in difficulty $\beta_{\text{male}} - \beta_{\text{female}}$. A positive value indicates a higher difficulty for males, whereas a negative value indicates a lower difficulty for males as opposed to females.

Gender: On average, male participants had a considerably higher physics competence (main effect = -0.594 logits, Cohen’s $d = -0.843$).⁶ Fourteen items (see Table 6) showed a DIF greater than 0.6 logits. Three items (phyn12t_c, phyn9t_c, and phyn2t_c) showed a very strong DIF reaching 1 logit.

Wave: On average, participants in the two waves basically did not differ in their physics competence (main effect = 0.020, Cohen’s $d = 0.028$). No item showed a DIF greater than 0.6 logits.

Books: On average, participants with many books at home performed better on the physics competence test (0-200 vs 201-500: main effect = 0.123, Cohen’s $d = 0.174$; 0-200 vs > 500: main effect = 0.327, Cohen’s $d = 0.464$; 201-500 vs > 500: main effect = 0.204, Cohen’s $d = 0.289$). Ten items (phyt1_c, phyh12_c, phyn7_c, phyn4_c, phyn13_c, phyb14_c, phye1_c, phyn12t_c, phyh5t_c, phyn9t_c) showed a DIF greater than 0.6 logits. Item phyn2t_c showed a very strong DIF exceeding 1 logit.

⁶ The variance of the Rasch model was used to estimate the effect size.

Table 6

Differential Item Functioning

| | Item | Gender | Wave | Books | | |
|----|----------|-------------------|--------|-------------------|------------------|--------|
| | | male vs female | 1 vs 2 | 0-200 vs > 500 | 201-500 vs > 500 | |
| 1 | phyh10_c | -0.228 | 0.024 | 0.086 | 0.040 | -0.046 |
| 2 | phyg1_c | 0.272 | -0.158 | -0.030 | -0.333 | -0.303 |
| 3 | phyn5_c | -0.252 | 0.116 | -0.171 | 0.081 | 0.252 |
| 4 | phyr1_c | -0.742 | -0.074 | -0.106 | 0.220 | 0.326 |
| 5 | phyg2_c | -0.328 | -0.112 | 0.098 | 0.323 | 0.225 |
| 6 | phye2_c | -0.096 | 0.118 | -0.111 | -0.246 | -0.135 |
| 7 | phyh8_c | -0.258 | 0.110 | -0.109 | 0.239 | 0.348 |
| 8 | phyn1_c | 0.756 | -0.382 | -0.093 | -0.018 | 0.075 |
| 9 | phyg8_c | -0.460 | -0.060 | -0.059 | 0.089 | 0.148 |
| 10 | phym14_c | 0.480 | -0.144 | 0.327 | 0.209 | -0.118 |
| 11 | phyt1_c | -0.158 | 0.134 | 0.616 | 0.056 | -0.560 |
| 12 | phyg6_c | 0.006 | 0.304 | 0.001 | 0.410 | 0.409 |
| 13 | phyh12_c | -0.062 | -0.334 | -0.413 | 0.269 | 0.682 |
| 14 | phyn12_c | -0.602 | -0.302 | 0.000 | 0.036 | 0.036 |

| Item | Gender | Wave | Books | | | |
|------|----------------|--------|------------------|----------------|------------------|--------|
| | male vs female | 1 vs 2 | 0-200 vs 201-500 | 0-200 vs > 500 | 201-500 vs > 500 | |
| 15 | phyh2_c | 0.288 | -0.160 | -0.120 | -0.123 | -0.003 |
| 16 | phyh5_c | 0.326 | -0.032 | -0.144 | -0.216 | -0.072 |
| 17 | phyn7_c | -0.368 | -0.060 | 0.402 | 0.957 | 0.555 |
| 18 | phyf3_c | 0.438 | -0.052 | -0.358 | -0.266 | 0.092 |
| 19 | phyb6_c | -0.350 | -0.006 | -0.204 | -0.114 | 0.090 |
| 20 | phyg4_c | 0.820 | -0.180 | 0.404 | -0.047 | -0.451 |
| 21 | phyn4_c | 0.214 | 0.384 | 0.868 | 0.801 | -0.067 |
| 22 | phyn10_c | 0.402 | 0.180 | -0.197 | -0.139 | 0.058 |
| 23 | phyf5_c | -0.556 | -0.092 | 0.216 | -0.300 | -0.516 |
| 24 | phyn13_c | 0.936 | 0.246 | -0.379 | -0.680 | -0.301 |
| 25 | phyb14_c | 0.634 | 0.366 | 0.767 | 0.499 | -0.268 |
| 26 | phyh6_c | 0.928 | 0.430 | -0.252 | -0.306 | -0.054 |
| 27 | phyn6_c | 0.226 | 0.174 | -0.043 | -0.362 | -0.319 |
| 28 | phyn15_c | 0.540 | -0.052 | -0.174 | -0.081 | 0.093 |
| 29 | phyt3_c | 0.406 | 0.180 | -0.168 | -0.301 | -0.133 |
| 30 | phyf1_c | 0.812 | -0.142 | -0.270 | -0.477 | -0.207 |

| | Item | Gender | Wave | Books | | |
|----|-----------|----------------|--------|------------------|----------------|------------------|
| | | male vs female | 1 vs 2 | 0-200 vs 201-500 | 0-200 vs > 500 | 201-500 vs > 500 |
| 31 | phye6_c | - | - | - | - | - |
| 32 | phye1_c | 0.256 | 0.014 | 0.290 | -0.323 | -0.613 |
| 33 | phyn9_c | 0.340 | 0.100 | 0.472 | -0.070 | -0.542 |
| 34 | phyo13_c | 0.046 | -0.248 | -0.179 | -0.464 | -0.285 |
| 35 | phyt13a_c | 0.510 | 0.316 | -0.526 | -0.536 | -0.010 |
| 36 | phyt13b_c | - | - | - | - | - |
| 37 | phyt13c_c | - | - | - | - | - |
| 38 | phyt13d_c | 0.832 | 0.090 | 0.173 | -0.059 | -0.232 |
| 39 | phyf9_c | 0.006 | 0.046 | -0.305 | 0.017 | 0.322 |
| 40 | phyf6_c | 0.000 | 0.192 | 0.095 | 0.079 | -0.016 |
| 41 | phyg13_c | - | - | - | - | - |
| 42 | phyn8_c | -0.328 | 0.128 | 0.077 | 0.322 | 0.245 |
| 43 | phyn14_c | -0.670 | -0.358 | -0.457 | -0.266 | 0.191 |
| 44 | phyt4a_c | -0.246 | -0.124 | 0.025 | -0.139 | -0.164 |
| 45 | phyt4b_c | 0.242 | 0.092 | -0.185 | -0.223 | -0.038 |
| 46 | phyt4c_c | 0.492 | 0.146 | -0.409 | -0.320 | 0.089 |

| | Item | Gender | Wave | Books | | |
|----|-----------|----------------|--------|------------------|----------------|------------------|
| | | male vs female | 1 vs 2 | 0-200 vs 201-500 | 0-200 vs > 500 | 201-500 vs > 500 |
| 47 | phyf7_c | 0.628 | 0.152 | -0.458 | -0.043 | 0.415 |
| 48 | phyb18_c | - | - | - | - | - |
| 49 | phyn3_c | -0.760 | -0.176 | -0.471 | 0.039 | 0.510 |
| 50 | phyn2_c | - | - | - | - | - |
| 51 | phyg5_c | 0.366 | 0.286 | 0.380 | 0.250 | -0.130 |
| 52 | phyt9_c | - | - | - | - | - |
| 53 | phyh3_c | -0.058 | -0.140 | -0.150 | -0.213 | -0.063 |
| 54 | phyb24_c | 0.058 | 0.234 | -0.132 | -0.222 | -0.090 |
| 55 | phyg19_c | -0.342 | -0.316 | -0.037 | 0.127 | 0.164 |
| 56 | phyf13_c | -0.322 | 0.284 | -0.248 | -0.220 | 0.028 |
| 57 | phyn11_c | -0.402 | 0.204 | 0.266 | 0.330 | 0.064 |
| 58 | phyf4_c | -0.300 | -0.214 | 0.195 | -0.126 | -0.321 |
| 59 | phyh15_c | 0.682 | -0.192 | 0.301 | 0.218 | -0.083 |
| 60 | phyn12t_c | -1.116 | -0.266 | 0.406 | 0.808 | 0.402 |
| 61 | phyh5t_c | -0.742 | 0.208 | 0.274 | 0.692 | 0.418 |
| 62 | phyh6t_c | -0.148 | -0.474 | 0.093 | 0.369 | 0.276 |

| | | Gender | Wave | Books | | |
|--------------------|----------|----------------|-------------|------------------|----------------|------------------|
| Item | | male vs female | 1 vs 2 | 0-200 vs 201-500 | 0-200 vs > 500 | 201-500 vs > 500 |
| 63 | phyn9t_c | -1.126 | 0.336 | 0.163 | -0.568 | -0.731 |
| 64 | phyn2t_c | -1.000 | -0.446 | 0.795 | 1.287 | 0.492 |
| main effect | | -0.594 | 0.020 | 0.123 | 0.327 | 0.204 |

In Table 7, the models with DIF are compared with those that included only the main effect of the respective variable. Regarding Akaike's (1974) information criterion (AIC), the more parsimonious models including only main effects were preferred over the ones containing the variables wave and books, but not gender. The Bayesian information criterion (BIC; Schwarz, 1978) takes into account the number of estimated parameters and thus prevents the overparameterization of models. Using BIC, the more complex model including DIF was preferred only for the variable gender.

Table 7

Comparison of Models With and Without DIF

| DIF variable | Model | Number of parameters | AIC | BIC |
|--------------|-------------|----------------------|-----------|-----------|
| Gender | main effect | 59 | 41,134.55 | 41,214.34 |
| | DIF | 116 | 40,941.45 | 41,098.32 |
| Wave | main effect | 59 | 41,401.68 | 41,481.47 |
| | DIF | 116 | 41,461.86 | 41,618.74 |
| Books | main effect | 60 | 34,395.33 | 34,476.47 |
| | DIF | 174 | 34,487.20 | 34,722.51 |

5.3.3 Rasch homogeneity

One essential assumption of the Rasch (1960) model is Rasch homogeneity. Rasch homogeneity implies that all item-discrimination parameters are equal. In order to test this assumption, a Birnbaum model (2PL; Birnbaum, 1968) was specified. In this model, discrimination parameters are freely estimated and not fixed to 1. The estimated discriminations differed across the items (see Table 5), ranging from 0.006 (item phyt13a_c) to 3.714 (item phyn2t_c). Despite the empirical preference for the 2PL (AIC = 41021.54, BIC = 41679.24, number of parameters = 115) model, the Rasch model (AIC = 41399.92, BIC = 41679.24, number of parameters = 58) more adequately matched the theoretical conceptions underlying the construction of the test (see Pohl & Carstensen, 2012, 2013 for a discussion of this issue). For this reason, the 1PL model was chosen as the scaling model.

6 Discussion

Descriptions and analyses presented in the previous sections were aimed at documenting the quality of the physics competence test used in the additional study Thuringia. The occurrence of different kinds of missing responses was evaluated, and item as well as test quality was examined. Furthermore, measurement invariance was examined for various grouping variables. The item fit statistics provided evidence of items with acceptable to good fit and some items that were measurement invariant across these subgroups (but see Table 6). The test was found to be reasonably reliable. As shown, ability estimates for participants with medium to good performance were found to be precise but less precise for low-performing participants.

7 Data in the Scientific Use File

The data in the Scientific Use File contain 64 items, all of which are scored as dichotomous variables with 0 indicating an incorrect response and 1 indicating a correct response. MC items are marked with a ‘_c’ at the end of the variable name. Appendix A provides the syntax that was used to generate the person estimates with the ConQuest 4.2 software (Wu, Adams, Wilson, & Haldane, 2007). Appendix B provides an alternative syntax for use with the TAM package (Robitzsch, Kiefer, & Wu, 2017) in the software R (R Core Team, 2017).

Manifest physics competence scores are provided in the form of WLEs (phy_sc1) along with their corresponding standard errors (phy_sc2). As described in Section 5, these person estimates were derived from the joint scaling of all two waves of the study. For persons who did not take the physics competence test, no WLE was estimated. WLEs were estimated for all items delivered in the Scientific Use File; except items with negative discriminations in the 2PL were excluded (items phy6_c, phyt13b_c, phyt13c_c, phyg13_c, phyb18_c, phyn2_c, and phyt9_c were excluded). Therefore, the delivered WLE is based on 57 items. In order to allow the users to estimate their own WLEs by considering different item selection standards, all test items are delivered in the Scientific Use File. For researchers interested in analyses that require one of the variables that showed $DIF > 0.6$ or 1 logits, we emphasize that (latent variable) models should be considered on the basis of partial measurement invariance (e.g. Byrne, Shavelson & Muthén, 1989).

We recommend the use of plausible values to investigate latent relationships between competence scores and other variables. Users interested in examining latent relationships may either include the measurement model in their analyses or estimate plausible values themselves. A description of these approaches can be found in Pohl and Carstensen (2012).

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Appendix

Appendix A: ConQuest Syntax for generating WLE estimates

title XXX;

datafile filename.dat;

format pid 1-7 responses 11-67;

labels << labels.nam;

codes 0,1;

model item;

set constraint=cases;

estimate ! stderr=empirical;

itanal ! form=long >> filename.itn;

export parameters >> filename.prm;

show cases ! estimates=wle >> filename.wle;

show ! estimates=latent, tables=1:2:3:4:5 >> filename.shw;

Appendix B: TAM Syntax for generating WLE estimates

```
setwd("Your/Working/Directory")

data <- # data read

items <- # column positions of the items in the SUF

library (TAM)

# Compute Rasch

RASCH <- tam(data[,items], irtmodel="Rasch", pid=data$id)

summary (RASCH)

# Compute 2 PL- Modell

TWOPL <- tam.mml.2pl(data[,items], irtmodel="2PL", pid=data$id)

summary (TWOPL)
```

Appendix C: Item Parameters based on all Items

Table S1

Item Parameters of the Physics Competence Test (all Items)

| | Item | Percentage correct | Difficulty/ location parameter | SE (difficulty/ location parameter) | WMNSQ | WMNSQ t-value | Correlation of item score with total score | Discrimination-2 PL |
|----|----------|--------------------|--------------------------------|-------------------------------------|-------|---------------|--|---------------------|
| 1 | phyh10_c | 16.22 | 1.769 | 0.061 | 0.97 | -0.9 | 0.37 | 1.109 |
| 2 | phyg1_c | 35.31 | 0.656 | 0.049 | 1.05 | 3.0 | 0.25 | 0.316 |
| 3 | phyn5_c | 42.96 | 0.306 | 0.047 | 0.94 | -4.7 | 0.48 | 1.644 |
| 4 | phyr1_c | 88.20 | -2.154 | 0.068 | 0.97 | -0.6 | 0.30 | 1.470 |
| 5 | phyg2_c | 60.93 | -0.484 | 0.047 | 0.98 | -1.6 | 0.42 | 1.134 |
| 6 | phye2_c | 60.47 | -0.467 | 0.048 | 0.99 | -0.5 | 0.36 | 0.829 |
| 7 | phyh8_c | 12.97 | 2.054 | 0.139 | 0.98 | -0.2 | 0.37 | 1.100 |
| 8 | phyn1_c | 28.80 | 0.956 | 0.106 | 1.05 | 1.0 | 0.30 | 0.480 |
| 9 | phyg8_c | 24.40 | 1.215 | 0.111 | 0.91 | -1.6 | 0.54 | 1.898 |
| 10 | phym14_c | 82.18 | -1.701 | 0.123 | 1.01 | 0.2 | 0.28 | 0.610 |
| 11 | phyt1_c | 39.45 | 0.435 | 0.098 | 0.97 | -1.1 | 0.45 | 1.133 |
| 12 | phyg6_c | 64.24 | -0.685 | 0.101 | 0.98 | -0.6 | 0.38 | 0.826 |

| | Item | Percentage correct | Difficulty/ location parameter | SE (difficulty/ location parameter) | WMNSQ | WMNSQ t-value | Correlation of item score with total score | Discrimination-2 PL |
|----|----------|--------------------|--------------------------------|-------------------------------------|-------|---------------|--|---------------------|
| 13 | phyh12_c | 16.49 | 1.726 | 0.131 | 0.97 | -0.3 | 0.40 | 1.313 |
| 14 | phyn12_c | 26.90 | 1.060 | 0.109 | 0.97 | -0.7 | 0.42 | 1.114 |
| 15 | phyh2_c | 38.78 | 0.463 | 0.100 | 0.99 | -0.2 | 0.39 | 0.810 |
| 16 | phyh5_c | 39.83 | 0.412 | 0.101 | 1.00 | 0.1 | 0.38 | 0.792 |
| 17 | phyn7_c | 39.63 | 0.429 | 0.100 | 0.96 | -1.1 | 0.46 | 1.083 |
| 18 | phyf3_c | 34.46 | 0.672 | 0.104 | 1.04 | 1.0 | 0.30 | 0.467 |
| 19 | phyb6_c | 16.60 | 1.753 | 0.128 | 0.99 | -0.1 | 0.35 | 0.932 |
| 20 | phyg4_c | 33.06 | 0.781 | 0.103 | 1.08 | 2.0 | 0.19 | 0.039 |
| 21 | phyn4_c | 11.44 | 2.210 | 0.150 | 1.01 | 0.1 | 0.20 | 0.425 |
| 22 | phyn10_c | 28.89 | 0.994 | 0.106 | 1.00 | 0.0 | 0.36 | 0.894 |
| 23 | phyf5_c | 46.57 | 0.163 | 0.097 | 1.00 | -0.1 | 0.39 | 0.812 |
| 24 | phyn13_c | 35.60 | 0.658 | 0.101 | 1.07 | 1.9 | 0.21 | 0.072 |
| 25 | phyb14_c | 9.62 | 2.398 | 0.165 | 1.02 | 0.2 | 0.09 | 0.130 |
| 26 | phyh6_c | 35.79 | 0.667 | 0.102 | 1.06 | 1.7 | 0.19 | 0.118 |
| 27 | phyn6_c | 37.80 | 0.573 | 0.103 | 1.01 | 0.3 | 0.33 | 0.699 |
| 28 | phyn15_c | 24.17 | 1.256 | 0.112 | 1.03 | 0.5 | 0.28 | 0.402 |
| 29 | phyt3_c | 31.55 | 0.867 | 0.104 | 1.01 | 0.3 | 0.29 | 0.363 |

| Item | Percentage correct | Difficulty/ location parameter | SE (difficulty/ location parameter) | WMNSQ | WMNSQ t-value | Correlation of item score with total score | Discrimination-2 PL | |
|------|--------------------|--------------------------------|-------------------------------------|-------|---------------|--|---------------------|--------|
| 30 | phyf1_c | 51.18 | -0.013 | 0.099 | 1.05 | 1.8 | 0.27 | 0.117 |
| 31 | phye6_c | 27.06 | 1.067 | 0.109 | 1.06 | 1.3 | 0.15 | -0.018 |
| 32 | phye1_c | 79.84 | -1.457 | 0.118 | 1.02 | 0.4 | 0.24 | 0.514 |
| 33 | phyn9_c | 50.67 | -0.028 | 0.101 | 1.05 | 2.1 | 0.25 | 0.216 |
| 34 | phyo13_c | 77.82 | -1.329 | 0.113 | 1.03 | 0.5 | 0.24 | 0.344 |
| 35 | phyt13a_c | 81.76 | -1.600 | 0.127 | 1.03 | 0.4 | 0.23 | 0.006 |
| 36 | phyt13b_c | 60.70 | -0.465 | 0.102 | 1.03 | 1.0 | 0.31 | -0.219 |
| 37 | phyt13c_c | 66.30 | -0.729 | 0.106 | 1.08 | 2.1 | 0.17 | -0.533 |
| 38 | phyt13d_c | 40.79 | 0.388 | 0.102 | 1.07 | 2.4 | 0.19 | 0.782 |
| 39 | phyf9_c | 19.69 | 1.492 | 0.124 | 0.99 | -0.1 | 0.30 | 0.902 |
| 40 | phyf6_c | 18.11 | 1.606 | 0.125 | 0.97 | -0.4 | 0.34 | 0.914 |
| 41 | phyg13_c | 60.04 | -0.441 | 0.098 | 1.09 | 3.1 | 0.13 | -0.256 |
| 42 | phyn8_c | 21.58 | 1.378 | 0.116 | 0.93 | -1.2 | 0.46 | 1.714 |
| 43 | phyn14_c | 33.75 | 0.724 | 0.102 | 0.97 | -0.9 | 0.40 | 1.098 |
| 44 | phyt4a_c | 74.95 | -1.171 | 0.112 | 1.00 | 0.1 | 0.31 | 0.604 |
| 45 | phyt4b_c | 62.96 | -0.569 | 0.102 | 1.04 | 1.3 | 0.26 | 0.587 |
| 46 | phyt4c_c | 22.43 | 1.334 | 0.116 | 1.04 | 0.7 | 0.19 | 0.263 |

| Item | Percentage correct | Difficulty/ location parameter | SE (difficulty/ location parameter) | WMNSQ | WMNSQ t-value | Correlation of item score with total score | Discrimination-2 PL | |
|------|--------------------|--------------------------------|-------------------------------------|-------|---------------|--|---------------------|--------|
| 47 | phyf7_c | 36.31 | 0.600 | 0.102 | 1.04 | 1.2 | 0.26 | 0.424 |
| 48 | phyb18_c | 31.89 | 0.808 | 0.107 | 1.11 | 2.7 | 0.09 | -0.358 |
| 49 | phyn3_c | 56.09 | -0.272 | 0.099 | 0.96 | -1.6 | 0.47 | 1.277 |
| 50 | phyn2_c | 28.28 | 0.993 | 0.112 | 1.09 | 1.7 | 0.16 | -0.024 |
| 51 | phyg5_c | 33.33 | 0.743 | 0.104 | 0.98 | -0.6 | 0.40 | 0.886 |
| 52 | phyt9_c | 44.75 | 0.220 | 0.100 | 1.10 | 3.7 | 0.16 | -0.092 |
| 53 | phyh3_c | 36.42 | 0.596 | 0.103 | 0.98 | -0.5 | 0.39 | 0.983 |
| 54 | phyb24_c | 14.98 | 1.876 | 0.135 | 1.02 | 0.3 | 0.28 | 0.702 |
| 55 | phyg19_c | 47.54 | 0.103 | 0.098 | 0.97 | -1.0 | 0.45 | 1.022 |
| 56 | phyf13_c | 50.42 | -0.029 | 0.099 | 0.94 | -2.3 | 0.51 | 1.565 |
| 57 | phyn11_c | 34.23 | 0.700 | 0.103 | 0.96 | -1.1 | 0.47 | 1.309 |
| 58 | phyf4_c | 24.47 | 1.220 | 0.114 | 0.97 | -0.5 | 0.45 | 1.373 |
| 59 | phyh15_c | 30.93 | 0.854 | 0.110 | 1.08 | 1.7 | 0.23 | 0.206 |
| 60 | phyn12t_c | 14.69 | 1.939 | 0.135 | 0.94 | -0.7 | 0.49 | 1.764 |
| 61 | phyh5t_c | 20.40 | 1.553 | 0.142 | 0.88 | -1.6 | 0.61 | 2.632 |
| 62 | phyh6t_c | 27.69 | 1.231 | 0.155 | 0.95 | -0.7 | 0.49 | 1.388 |
| 63 | phyn9t_c | 10.43 | 2.563 | 0.236 | 0.99 | 0.0 | 0.45 | 1.668 |

| | | | <i>SE</i> (difficulty/ location parameter) | WMNSQ | WMNSQ t-value | Correlation of item score with total score | Discrimination- 2 PL |
|----|----------|-------|---|-------|------------------|--|-------------------------|
| 64 | phyn2t_c | 12.77 | 2.245 | 0.90 | -0.6 | 0.62 | 3.714 |

Appendix D: Content Area for each Item

Table S2.
Content Area for each Items

| | Item | Content Area | | Item | Content Area |
|----|-------------|---|----|-------------|---|
| 1 | phyh10_c | Electrical fields and inter-dependency | 33 | phyn9_c | Optics |
| 2 | phyg1_c | Magnetic fields and electromagnetic induction | 34 | phyo13_c | Dynamics: Mechanics of the Rigid Body |
| 3 | phyn5_c | Waves | 35 | phyt13a_c | Thermodynamics |
| 4 | phyr1_c | Optics | 36 | phyt13b_c | Thermodynamics |
| 5 | phyg2_c | Thermodynamics | 37 | phyt13c_c | Thermodynamics |
| 6 | phye2_c | Thermodynamics | 38 | phyt13d_c | Thermodynamics |
| 7 | phyh8_c | Electrical fields and inter-dependency | 39 | phyf9_c | Thermodynamics |
| 8 | phyn1_c | Magnetic fields and electromagnetic induction | 40 | phyf6_c | Magnetic fields and electromagnetic induction |
| 9 | phyg8_c | Waves | 41 | phyg13_c | Waves |
| 10 | phym14_c | Optics | 42 | phyn8_c | Optics |
| 11 | phyt1_c | Thermodynamics | 43 | phyn14_c | Dynamics: Mechanics of the Rigid Body |
| 12 | phyg6_c | Thermodynamics | 44 | phyt4a_c | Thermodynamics |
| 13 | phyh12_c | Waves | 45 | phyt4b_c | Thermodynamics |
| 14 | phyn12_c | Dynamics: Mechanics of the Rigid Body | 46 | phyt4c_c | Thermodynamics |
| 15 | phyh2_c | Thermodynamics | 47 | phyf7_c | Quantum physics: Quanta and matter |
| 16 | phyh5_c | Special Theory of Relativity | 48 | phyb18_c | Electrical fields and inter-dependency |
| 17 | phyn7_c | Waves | 49 | phyn3_c | Waves |
| 18 | phyf3_c | Quantum physics: Quanta and matter | 50 | phyn2_c | Magnetic fields and electromagnetic induction |
| 19 | phyb6_c | Electrical fields and inter-dependency | 51 | phyg5_c | Optics |

Table S2.
Content Area for each Items

| Item | Content Area | Item | Content Area | | |
|-------------|---------------------|---|---------------------|-----------|---|
| Item | Content Area | Item | Content Area | | |
| 20 | phyg4_c | Magnetic fields and electromagnetic induction | 52 | phyt9_c | Thermodynamics |
| 21 | phyn4_c | Magnetic fields and electromagnetic induction | 53 | phyh3_c | Quantum physics: Quanta and matter |
| 22 | phyn10_c | Optics | 54 | phyb24_c | Magnetic fields and electromagnetic induction |
| 23 | phyf5_c | Thermodynamics | 55 | phyg19_c | Magnetic fields and electromagnetic induction |
| 24 | phyn13_c | Dynamics: Mechanics of the Rigid Body | 56 | phyf13_c | Waves |
| 25 | phyb14_c | Electrical fields and interdependency | 57 | phyn11_c | Optics |
| 26 | phyh6_c | Magnetic fields and electromagnetic induction | 58 | phyf4_c | Dynamics: Mechanics of the Rigid Body |
| 27 | phyn6_c | Magnetic fields and electromagnetic induction | 59 | phyh15_c | Quantum physics: Quanta and matter |
| 28 | phyn15_c | Dynamics: Mechanics of the Rigid Body | 60 | phyn12t_c | Dynamics: Mechanics of the Rigid Body |
| 29 | phyt3_c | Thermodynamics | 61 | phyh5t_c | Special Theory of Relativity |
| 30 | phyf1_c | Quantum physics: Quanta and matter | 62 | phyh6t_c | Magnetic fields and electromagnetic induction |
| 31 | phye6_c | Electrical fields and interdependency | 63 | phyn9t_c | Optics |
| 32 | phye1_c | Waves | 64 | phyn2t_c | Magnetic fields and electromagnetic induction |